

Exact Gap Computation for Code Coverage Metrics

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Motivation

- test generation + test data selection difficult
- code coverage metrics: estimate quality of test suites
- coverage 100% → quality fine
- practice: 100% impossible (e.g. dead code)
- tester improve test suite: Is adding an extra test wise?
- Question: What is the maximal possible coverage?
- presented here: framework to answer this exactly

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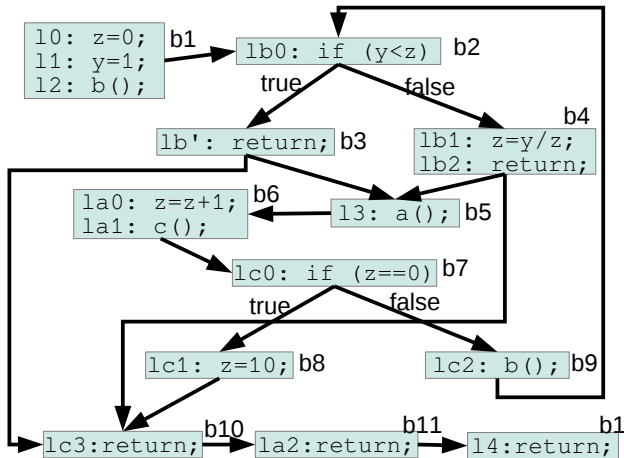
char y,z;
void b() {
  lb0: if(y<z) return
  lb1: z=y/z;
  lb2: return; }

void c() {
  lc0: if (z == 0)
    lc1: z = 10;
  else lc2: b();
  lc3: return; }

void a() {
  la0: z=z+1;
  la1: c();
  la2: return; }

void main() {
  l0: z=0;
  l1: y=1;
  l2: b();
  l3: a();
  l4: return; }

```



Example P_1 in ISO-C syntax and corresponding BBI-CFG

nodes: $blocks(P)$, $edges(P)$: interprocedural control flow

Code Coverage Metrics γ

- test suite $t \in T_P$: set of tests $t = \{\alpha_1, \alpha_2, \dots\}$ for program P
- code coverage metric $\gamma : T_P \rightarrow [0, 1]$ monotonically increasing
- function coverage $\gamma_f^P(t) := |\text{func}(t)|/|\text{func}(P)|$
- statement coverage $\gamma_s^P(t) := |\text{stats}(t)|/|\text{stats}(P)|$
- decision coverage $\gamma_d^P(t) := |\text{edges}(t)|/|\text{edges}(P)|$
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- $bExpr(I) = \{e_1, e_2, \dots, e_n\}$... set of all boolean sub-expressions
- $BExpr(P) := \{(l, e) \bullet l \in \text{labels}(P), e \in bExpr(l)\}$
- condition or predicate coverage metric:
 $\gamma_c^P(t) := |\text{exval}(t, P)|/(2 \cdot |BExpr(P)|)$

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Code Coverage Metric Gap δ

- let $\gamma : T_P \rightarrow [0, 1]$ be a code coverage metric
- code coverage metric gap $\delta_\gamma(P) := \inf_{t \in T_P} (1 - \gamma(t))$
- smallest diff.: practical coverage ratio vs. theoretical maximum
- not computable in Turing powerful languages
- more expressive model \rightarrow more accurate computat. of gap δ_γ
 \rightarrow adequate modeling

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Suitable Models (basic statements)

- **symbolic pushdown system (SPDS): ISO-C compatible semantic**
- describe SPDS by ISO-C syntax (platform-specific semantic)
 $e \in Expr, "l : s" \in stats$, s has the following forms:
 - * $x[e_1] = e_2$; writing $\llbracket e_2 \rrbracket$ into variable x at index $\llbracket e_1 \rrbracket$
 - * $f(x_1, \dots, x_n)$; function call (call by value)
 - * $return$; function return
 - * $if (e) goto l$; conditional jump to $l \in labels$
- not Turing powerful (infinite Kripke structure)

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Symbolic Pushdown System (SPDS)

- **SPDS S** : global variables $vgbl$, functions $func$, $main \in func$
- variable x (array) has integer type $bits(x)$ and length $len(x)$
- each statement has unique label $l \in labels(S)$
- $fst(f)$ is first label of function f
- state of S : configuration $(g, [(l, c)...])$ – current execute label l
- $g : vgbl \times \mathbb{Z} \rightarrow \mathbb{Z}$, $c : vlcl(l) \times \mathbb{Z} \rightarrow \mathbb{Z}$...variable settings
- $g(x, i), c(x, i)$ current value of variable x on index i

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Exact Gap Computation Framework

Given: program P + code coverage metric $\gamma : T_P \rightarrow [0, 1]$

- 1 Create SPDS S with ISO-C compatible semantic for P
- 2 Modify S to S' to enable gap analysis
- 3 Compute exact variable ranges for the new variables in S'
- 4 Conclude exact size of the gap $\delta_\gamma(S)$
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Step 1 - SPDS Modeling

- **map ISO-C statements to basic statements (abbreviations)**
- other languages similar (e.g. Java using JMoped)
- higher level concepts can be simulated... (see paper)

- **map ISO-C expressions to basic expressions**
 - expressions as parameters, evaluate to temporary variables
 - return expressions, new global variable (only for function)
 - function call to expression, intermediate compiler rewrites to further concepts
 - unconditional jump, skip statement, without parameter, conditional statements, local variable definitions, loops (do, while, for), modular arithmetic/integer overflow, dynamic memory, pointers, call by reference, dynamic arrays
- recursion bounded; call by reference + local variables in heap

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 - omit returns and labels: introduced during interpretation
 - expressions as parameters: evaluate to temporary variables
 - return expressions: new global variable (not for language)
 - call by reference: evaluate intermediate compiler expressions
 - loops: conditional, unconditional, simple, complex, with parameters, conditional statements, local variable definitions
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- map ISO-C statements to basic statements (abbreviations)
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Step 3 - Extraction of Exact Variable Ranges

- model checker Moped: algorithm to create $Post^*$ automaton
 - $Post^*$ accepts reachable configurations (infinite set)
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char y,z; bool x;
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- new variable x with $bits(x) = len(x) = 1$

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$\rightarrow range_f^{S'}(x) = \emptyset \Leftrightarrow f \notin \{l0, l1, l2, lb0, lb1\}$

$$\Rightarrow \delta_s(S) = 1 - \frac{|\{l \in \text{state}(S) * range_f^{S'}(x) \neq \emptyset\}|}{|\text{state}(S)|} = 67\%$$

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$$\Rightarrow \delta_s(S) = 1 - \frac{|\{l:s \in stats(S) \bullet range_I^{S'}(x) \neq \emptyset\}|}{|stats(S)|} = 67\%$$

$$\Rightarrow \delta_f(S) = 1 - \frac{|\{f \in func(S) \bullet range_{fst(f)}^{S'}(x) \neq \emptyset\}|}{|func(S)|} = 50\%$$

$$\Rightarrow \delta_b(S) = 1 - \frac{|\{b \in blocks(S) \bullet range_{fst(b)}^{S'}(x) \neq \emptyset\}|}{|blocks(S)|} = 75\%$$

- no test suite t with branch coverage $\gamma_b^S(t) > 25\%$

Step 2+4 - $\delta_f(S)$, $\delta_s(S)$ and $\delta_b(S)$ illustration

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char y,z; bool x;
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Step 2+4 - SPDS Supplementation and Exact Gap Inference

Decision coverage gap $\delta_d(S)$

- **decision coverage: fraction of edges $(a, b) \in \text{edges}(S)$**
- remember last executed basic block using ...
- ...new global variable $x \notin \text{vgbl}(S) \rightsquigarrow \text{SPDS } S'$
- $\text{len}(x) = 1, \text{bits}(x) = 1 + \lceil \log_2(|\text{blocks}(S)|) \rceil$
- each block b has unique number n_b
- " $l : s$ " $\in \text{stats}(S) \Rightarrow "$ $l : x = n_{\text{block}(l)}; l' : s;$ "

$$\Rightarrow \delta_d(S) = 1 - \frac{|\{(a,b) \in \text{edges}(S) * n_b \in \text{range}_{\text{bit}(b)}^S(x)\}|}{|\text{edges}(S)|}$$

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Step 2+4 - SPDS Supplementation and Exact Gap Inference

Decision coverage gap $\delta_d(S)$

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Step 2+4 - Decision coverage gap $\delta_d(S)$ illustration

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char y,z;
void b() {
  lb0: if(y<z) return
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```
void c() {
  lc0: if (z == 0)
    lc1: z = 10;
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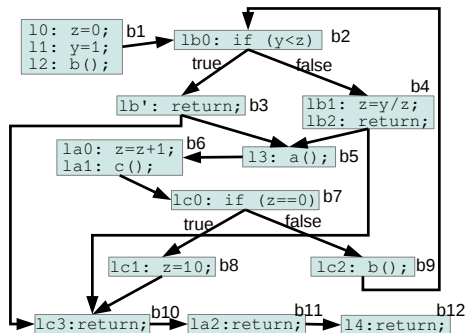
```

```
void a() {
  la0: z=z+1;
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  la2: return; }

```

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void main() {
  l0: z=0;
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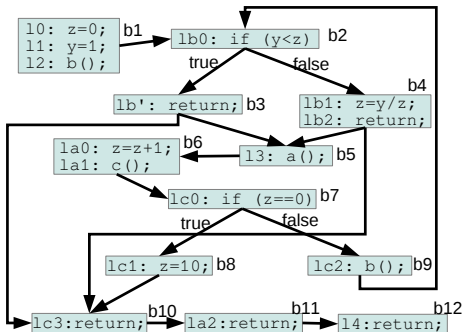
Step 2+4 - Decision coverage gap $\delta_d(S)$ illustration

```
char y,z; int x(4);
void b() {
  lb0: x=2; if (y<z){ x=3; return;}
  lb1: x=4; z=y/z;
  lb2: return; }
```

```
void c() {
  lc0: x=7; if (z == 0)
    lc1: x=8; z = 10;
  else lc2: x=9; b();
  lc3: x=10; return; }
```

```
void a() {
  la0: x=6; z=z+1;
  la1: c();
  la2: x=11; return; }
```

```
void main() {
  l0: x=1; z=0;
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  l2: b();
  l3: x=5; a();
  l4: x=12; return; }
```



- value of x represents incoming block nr
- exact $range_{l_j}^{S'}(x)$ indicates incoming blocks
- decision coverage gap $\delta_d(S) = 87\%$
- only 13% of the CFG edges are coverable

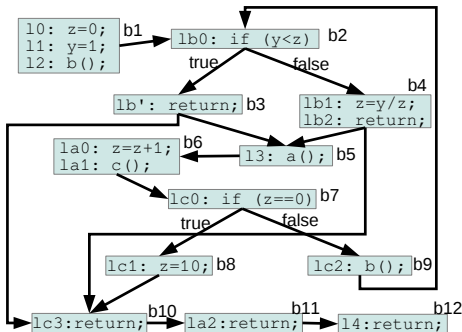
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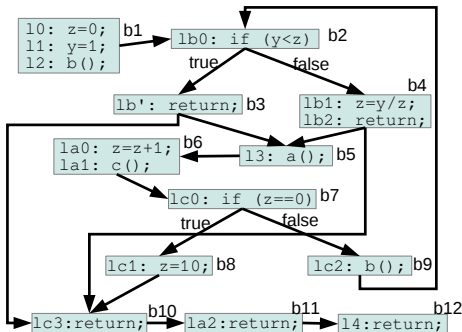
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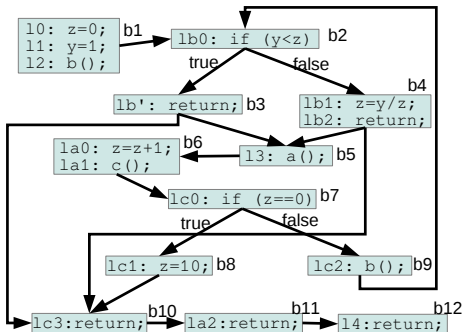
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Step 2+4 - SPDS Supplementation and Exact Gap Inference

Condition coverage gap $\delta_c(S)$

- consider every boolean sub-expression e in *SPDS* S
- new global variables $x_e \notin \text{vgbl}(S) \rightsquigarrow \text{SPDS } S'$
- $\text{len}(x_e) = 1, \text{bits}(x_e) = 1$
- " $l : s$ " \Rightarrow " $l : x_{e_1} = e_1; x_{e_2} = e_2; \dots x_{e_n} = e_n; l' : s;$ "
- evaluations of x_{e_i} equivalent to covered conditions e_i

$$\Rightarrow \delta_c(S) = 1 - \frac{\sum_{\substack{l \in \text{Labels}(S) \\ e \in \text{bExpr}(l)}} |\text{range}_{S'}^e(x_e)|}{2 \cdot |\text{BExpr}(S)|}$$

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Step 2+4 - Condition coverage gap $\delta_c(S)$ illustration

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Step 2+4 - Condition coverage gap $\delta_c(S)$ illustration

```

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- **exact** $\text{range}_p^{S'}(x) \subseteq \{\text{true}, \text{false}\}$
 - $\text{range}_p^{S'}(x) = \{\text{false}\}$ indicates $y < z$ evals.
 - $\text{range}_q^{S'}(x) = \emptyset$ indicates $z == 0$ evals.
- condition coverage gap $\delta_c(S) = 75\%$
 → only 25% of the conditions are coverable

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- condition coverage gap $\delta_c(S) = 75\%$
 → only 25% of the conditions are coverable

Step 2+4 - Condition coverage gap $\delta_c(S)$ illustration

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char y,z; bool x;
void b() {
  lb0: x=(y<z); p: if (y<z) return ;
  lb1: z=y/z;
  lb2: return ; }

void c() {
  lc0: x=(z==0); q: if (z == 0)
    lc1: z = 10;
  else lc2: b();
  lc3: return ; }

void a() {
  la0: z=z+1;
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  la2: return ; }

void main() {
  l0: z=0;
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  l4: return ; }

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- program P equivalent to SPDS $S \rightarrow$ exact gaps
- program P abstracted to SPDS $S \rightarrow$ approximated gaps
- more practical: approximate $range_I(x) \rightarrow$ approximated gaps
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$$\Rightarrow \delta_\gamma^+ \leq \delta_\gamma \leq \delta_\gamma^-$$

- perfect approximation: $\delta_\gamma^+ = \delta_\gamma^-$
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- ISO-C programs mapped to symbolic pushdown systems
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- in a similar way: linear code sequence and jump coverage, jj-path/path coverage, entry/exit or loop coverage

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Questions?